

Application for United States Letters Patent  
for  
**Combined Pre-Equalizer and Nyquist Filter**

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## Field

Embodiments of the present invention relate to digital signal processing, and more particularly, digital signal processing for a cable modem.

## Background

5 Cable modems allow for communicating via CATV (Community Access Television) coaxial cable. Specifications for cable modems are published under the auspices of Cable Television Laboratories, also known as CableLabs®, [www.cablelabs.com](http://www.cablelabs.com), a non-profit research and development consortium of cable system operators. Fig. 1 illustrates a functional block diagram for the physical layer of a prior art  
10 cable modem according to DOCSIS (Data Over Cable Service Interface Specification), see CableLabs.

In Fig. 1, block framer **102** frames digital data, and provides these frames to Reed-Solomon encoder **104**. Randomizer **106** reduces any constant component (e.g., a string of zeros) in the output of Reed-Solomon encoder **104**. Preamble **108** provides a  
15 training sequence, used by a receiver at the head end (not shown) for TDMA (Time Division Multiple Access) communication. Symbol map **110** maps digital data to a symbol chosen from a 16QAM (Quadrature Amplitude Modulation) signal constellation. Each of these symbols may be represented by 2 bits for the I (In-phase) component and 2 bits for the Q (Quadrature) component. Nyquist filter **112** filters the digital output from  
20 symbol map **110** so as to reduce ISI (Inter-Symbol Interference). Modulator **114** up-converts the digital signal, and digital-to-analog **116** converts the digital signal to an analog signal. Cable interface **118** provides the proper interface to cable **120**.

Nyquist filter **112** is a real-valued digital filter. Nyquist filter **112** provides interpolation, so that the time spacing of a discrete-time signal at the output of Nyquist  
25 filter **112** is less than the time spacing of a discrete-time signal at its input. An embodiment of Nyquist filter **112** is illustrated in Fig. 2, where Nyquist filter **112** is implemented as a FIR (Finite Impulse Response) filter, and the interpolation is such that if the time spacing of a discrete-time signal to the input of Nyquist filter **112** is denoted by  $T$ , then the time spacing of a discrete-time signal at its output is  $T/4$ . The filter of Fig.  
30 2 is implemented as a tap delay line, with unit delay elements **202**. The filter tap weights are denoted by  $c(i), i = 0, 1, \dots, N - 1$ , where  $N$  is the filter length. Adder unit **202** adds

the weighted results to provide the filtered output. Interpolation element **206** indicates that three zeroes are inserted for each input data symbol. In practice, there would be one filter for the in-phase component and one filter for the quadrature component, but for simplicity, only one filter is illustrated in Fig. 2.

A change to the cable modem standard DOCSIS (Radio Frequency Interface Specification, SP-RFIV1.1-I02-990731) requires that a transmit pre-equalizer be supported in a cable modem at subscriber locations. The output of Nyquist filter **112** for some embodiments is 10 bits, and consequently applying a pre-equalizer to the output of Nyquist filter **112** would require 10 bit by 10 bit multiplication, and this substantial increase in numerical processing leads to an increase in die area to perform the transmit pre-equalization. Consequently, there is a need to provide practical implementations of a pre-equalizer in a cable modem without substantially increasing die area.

### **Brief Description of the Drawings**

Fig. 1 is a functional diagram of a cable modem.

Fig. 2 is a Nyquist filter.

Fig. 3 is a flow diagram for obtaining the in-phase and quadrature filter coefficients of an embodiment of the invention.

Fig. 4 is a filter for Nyquist filtering and pre-equalization according to an embodiment of the invention to obtain in-phase components.

Fig. 5 is a filter for Nyquist filtering and pre-equalization according to an embodiment of the invention to obtain quadrature components.

Fig. 6 is another filter structure for a sub-block of the filter in Fig. 5.

Fig. 7 illustrates a computer system employing an embodiment of the present invention.

### **Description of Embodiments**

Embodiments according to the present invention provide efficient pre-equalization by combining a pre-equalizer with a Nyquist filter. Combining pre-equalization with Nyquist filtering results in a filter structure having no more inherent complexity than a Nyquist filter by itself. In particular, the numerical computations involved in filter weight multiplication are no more involved than performing Nyquist filtering by itself.

A flow diagram illustrating the synthesis of the combined filter is provided in Fig.

3. For box **302** a pre-equalizer is synthesized as an FIR filter having impulse response (filter weights)  $g(i) = g_I(i) + jg_Q(i), i = 0, 1, \dots, L-1$ , where  $g_I(i)$  are the in-phase components of the filter weights  $g(i)$  and  $g_Q(i)$  are the quadrature components of the filter weights  $g(i)$ . This synthesis may be accomplished by any well-known technique, such as measuring the impulse response of the cable channel and equalizing accordingly.

For box **304**, given the Nyquist filter impulse response  $c(i), i = 0, 1, \dots, N-1$ , the combined filter, denoted as  $c'(i) = c'_I(i) + jc'_Q(i), i = 0, 1, \dots, N+L-2$ , is given by

$$c' = g * c, \text{ where } * \text{ denotes convolution. That is, } c'(i) = \sum_{k=0}^{L-1} g(k)c(i-k), \text{ where it is}$$

understood that  $c(i) = 0$  for  $i < 0$  or  $i > N-1$ . For the embodiment of Fig. 3, the  $c(i)$  are real-valued, so that  $c'_I = g_I * c$  and  $c'_Q = g_Q * c$ .

The embodiment of Fig. 4 may be employed to obtain the in-phase components for Nyquist and pre-equalized filtered output data in which the combined filter weights are given as indicated in the flow diagram of Fig. 3. Similarly, the embodiment of Fig. 5 may be employed to obtain the quadrature component for the output data.

The in-phase and quadrature components of the input discrete-time signal to the filters of Figs. 4 and 5 are each 2 bits. Multipliers **406** and **506** in Figs. 4 and 5 need only perform 2 bit by J bit multiplication, where J is the word length of the filtered output in bits. For example, in one embodiment, the in-phase and quadrature inputs to modulator **114** are 10 bits, so that the filter weights in Figs. 4 and 5 are 10 bits and multipliers **406** and **506** perform 2 bit by 10 bit multiplication. Multiplication by a 2 bit number is relatively easy to implement in hardware, requiring only a bit shift followed by addition. Note that if Nyquist filtering and pre-equalization are not combined as described in Fig. 3, but instead pre-equalization is performed after Nyquist filtering, then providing 10 bit outputs would require 10 bit by 10 bit multiplication, which is more costly than simple 2 bit by 10 bit multiplication.

As described before, interpolation elements **404** and **504** in Fig. 4 and 5 insert three zeros for each received sample of the input discrete-time signal, so that the resulting filtered output is provided at four times the data rate as the input to the filter. Adders **402**

and **502** in Figs. 4 and 5 add the resulting 10 bit numbers from multipliers **406** and **506** to provide the filtered output. Adders **402** and **502** also round the resulting addition, so that the final output has J bit word length, where in one embodiment,  $J = 10$ .

Various other known filter structures may be employed to perform combined  
5 Nyquist filtering and pre-equalization. For example, Fig. 6 is an alternative filter implementation for sub-block **406** of Fig. 4, where in Fig. 6  $N' = N - L - 1$ . Filters similar in structure to that of Fig. 6 may also be used for other sub-blocks (not shown) in Figs. 4 and 5. The filter structure of Fig. 6 has several advantages over that of Fig. 4. Multipliers **602** in Fig. 6 operate at the input data rate, whereas multipliers **406** in Fig. 4  
10 operate at four times the input data rate. Similarly, adders **604** operate at the input data rate. Multiplexer **606**, however, operates at four times the input data rate, and multiplexes the output of sub-blocks **608** to provide an output signal at four times the input data rate. Because of round-off errors, the filter of Fig. 6 will often not be numerically identical to that of Fig. 4. Another important advantage of the filter in Fig. 6 is the savings in delay  
15 elements **610**. The filter in Fig. 6 has approximately one-fourth as many delay elements as sub-block **406** in Fig. 4. Many other well-known filter structures may be utilized to perform the filtering indicated in Fig. 4, although the final filtered output may not be identical to that of Fig. 4 due to round off error.

Embodiments of the present invention may be employed in many devices and  
20 systems. One such system is illustrated in Fig. 7, where computer system **702** comprises central processing unit (CPU) **704**, chipset **706**, system memory **708**, and system bus **710**. Modem **712** is coupled to a cable (not shown) through cable interface **118**, and is coupled to system bus **710** to communicate with CPU **704**.

Clearly, various modifications may be made to the disclosed embodiments  
25 without departing from the scope of the invention as claimed below.